

TRENDS IN INTERNATIONAL MATHEMATICS AND SCIENCE STUDY

TIMSS



TIMSS 2007 International Mathematics Report

*Findings from IEA's Trends in
International Mathematics and
Science Study at the Fourth
and Eighth Grades*

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TIMSS & PIRLS
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Lynch School of Education, Boston College

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